

Along axis,

$$B = \frac{\mu_0 I}{2} \frac{R^2}{(R^2 + z^2)^{3/2}}$$

radius of loop  $\downarrow$   $R^2$

$\uparrow$   $2$

$\swarrow$   $(R^2 + z^2)^{3/2}$  distance from loop

no  $\pi$  in this equation

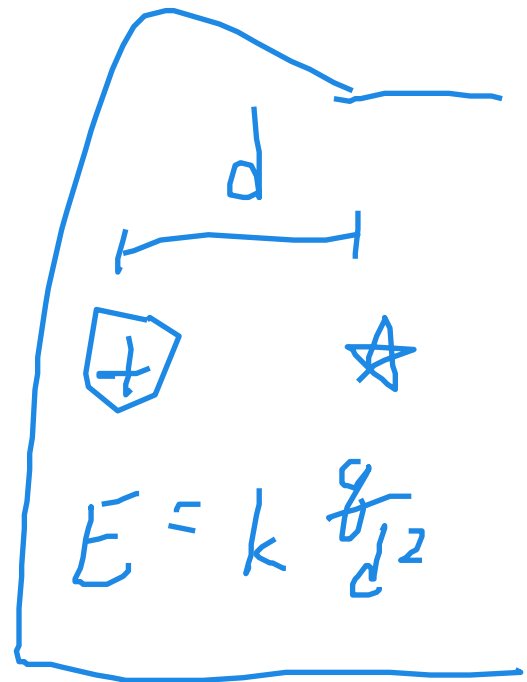
Very far away

$$z \gg R$$

$$R^2 + z^2 \approx z^2$$

$$B \approx \frac{\mu_0 I R^2}{2 (z^2)^{3/2}}$$

$$\approx \frac{\mu_0 I R^2}{2 z^3}$$



Fields of magnetic dipoles die away  
as  $\frac{1}{(\text{distance})^3}$ , faster than  $\frac{1}{(\text{distance})^2}$

Current Loops are like

Bar magnets —  
both dipoles

"Strength" of a Dipole

Magnetic Dipole Moment

$\vec{\mu}$

For a bar magnet

$\vec{\mu}$  points from  
S to N

Magnitude is  
just given

For a current loop

- direction from  
RHR circle:  $\vec{\mu}$   
thumb:  $\vec{\mu}$

$$|\vec{\mu}| = I A = I \pi R^2$$

circle                  for circle

Far away on axis of  
a dipole

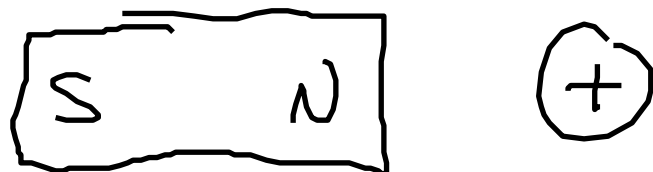
$$B = \frac{\mu_0 I \pi R^2}{2\pi z^3}$$

constant

$$\vec{B} = \frac{\mu_0 \vec{\mu}}{2\pi z^3}$$

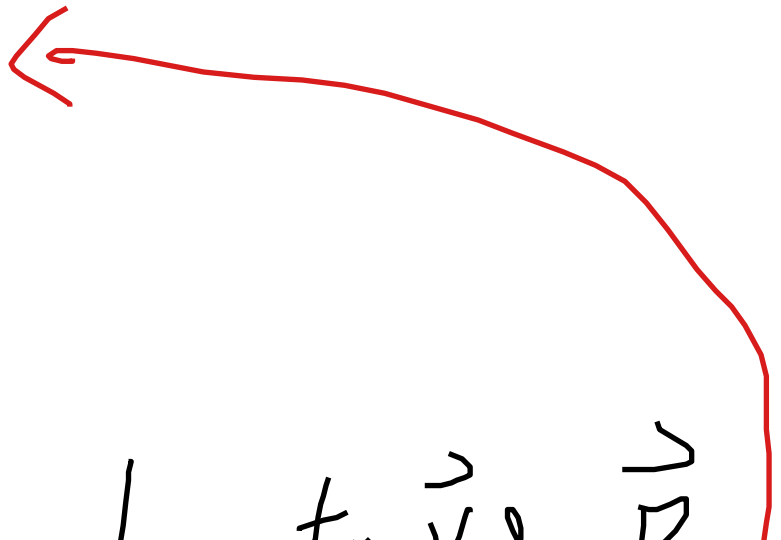
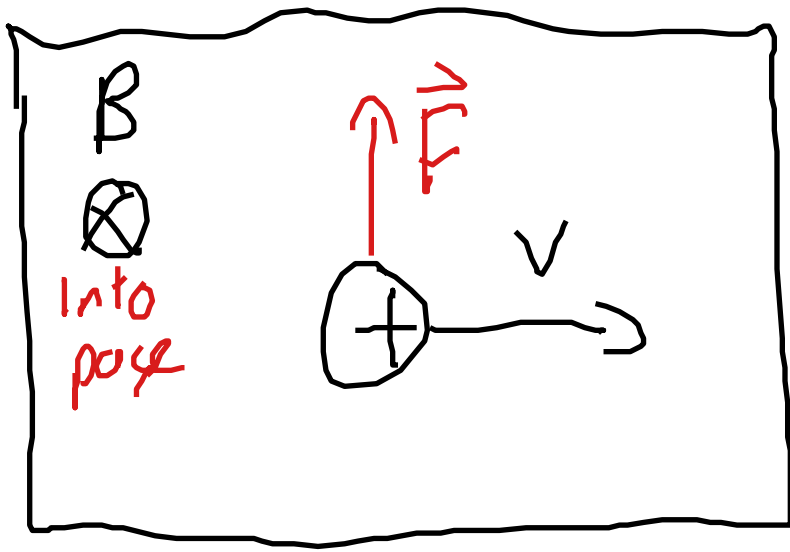
magnetic dipole moment

Static charges do  
not care about  $\vec{B}$



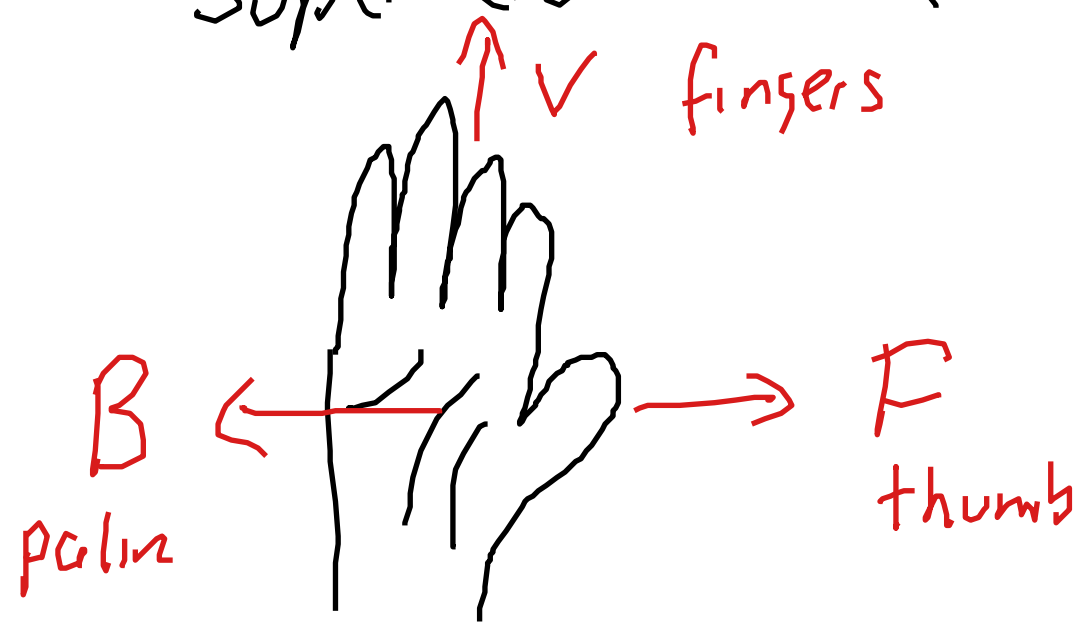
nothing  
happens

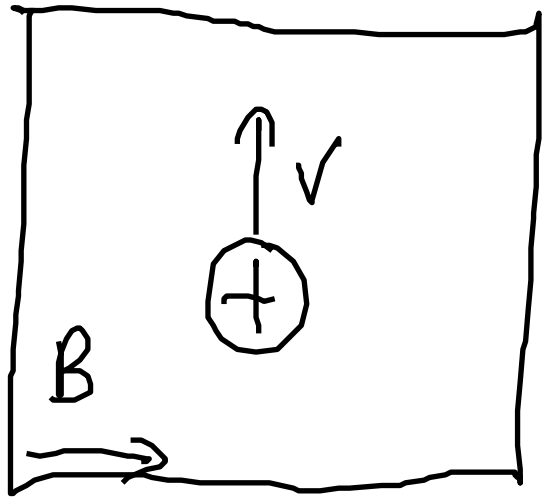
Moving charges feel a force  
in a  $\vec{B}$  field



- $\vec{F}$  is always  $\perp$  to  $\vec{v}$  &  $\vec{B}$
- To choose which direction (up or down)

Superhero RHR



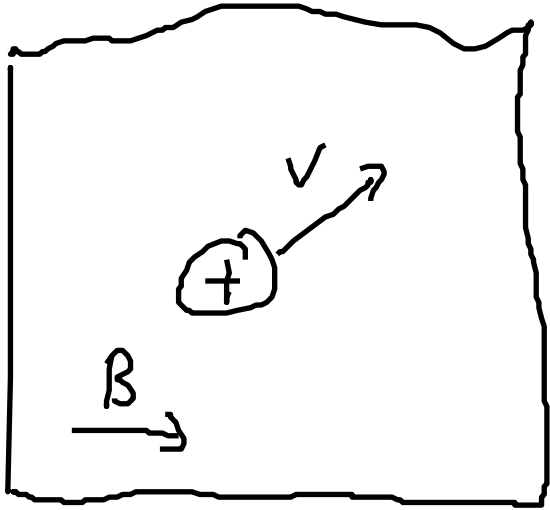


What is  $F$ ?

• can't be  $\uparrow$  or  $\downarrow$   
(b/c  $\perp$  to  $v$ )

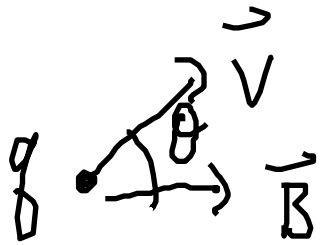
• can't be  $\rightarrow$  or  $\leftarrow$   
(b/c  $\perp$  to  $B$ )

therefore  $\odot$  out or  $\otimes$  in



• either  $\odot$  or  $\otimes$   
 (perpendicular to the  
 plane of  $\vec{v}$  &  $\vec{B}$ )

•  $\vec{F}$  is still  $\otimes$



$$|\vec{F}| = q v B \sin \theta$$

$$\theta = 0$$

$$\vec{v} \rightarrow$$

$$\vec{B} \rightarrow$$

$$\sin \theta = 0$$

$$F = 0$$

$$\theta = 90^\circ$$

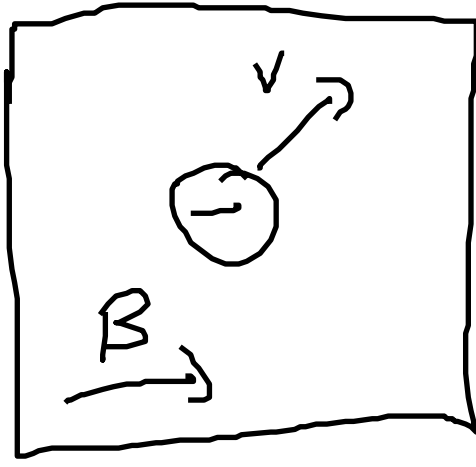
$$\vec{B} \uparrow$$

$$\vec{v} \rightarrow$$

$$\sin 90^\circ = 1$$

$$F = q v B$$





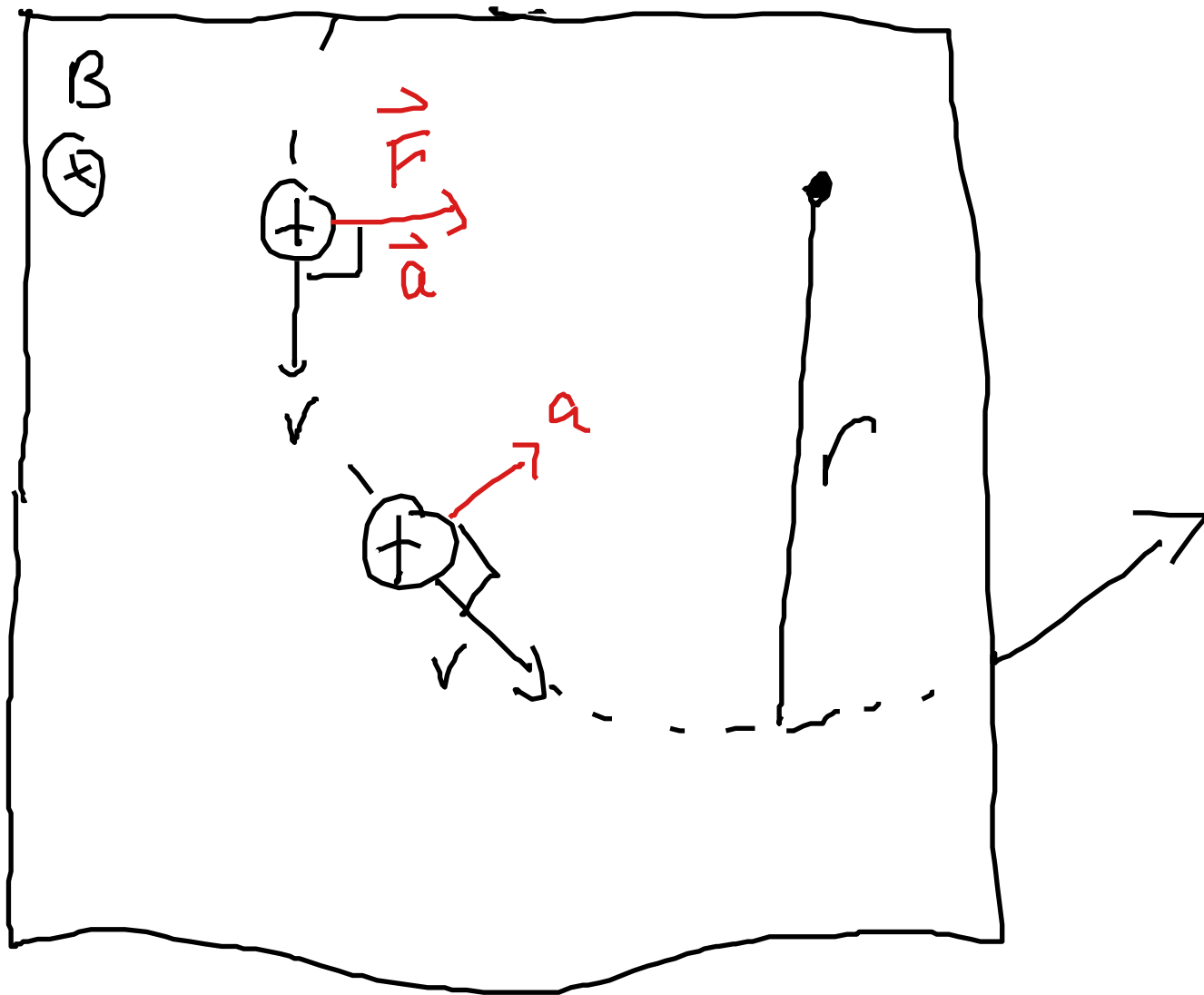
$\vec{F}$   $\odot$  out of page

(opposite  $\oplus$ )

Negative charges feel force in opposite direction

- electron twist

- LHR



Uniform Circular Motion

$$r = \frac{mv}{qB}$$

radius