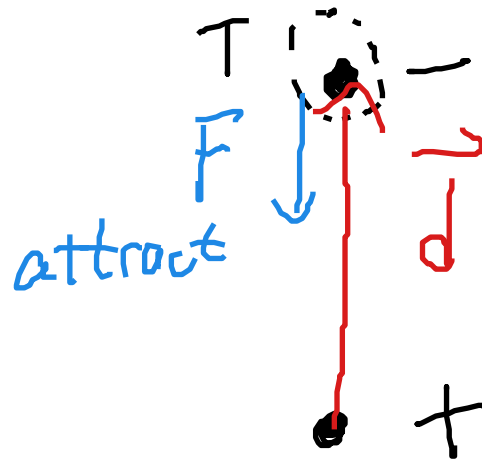
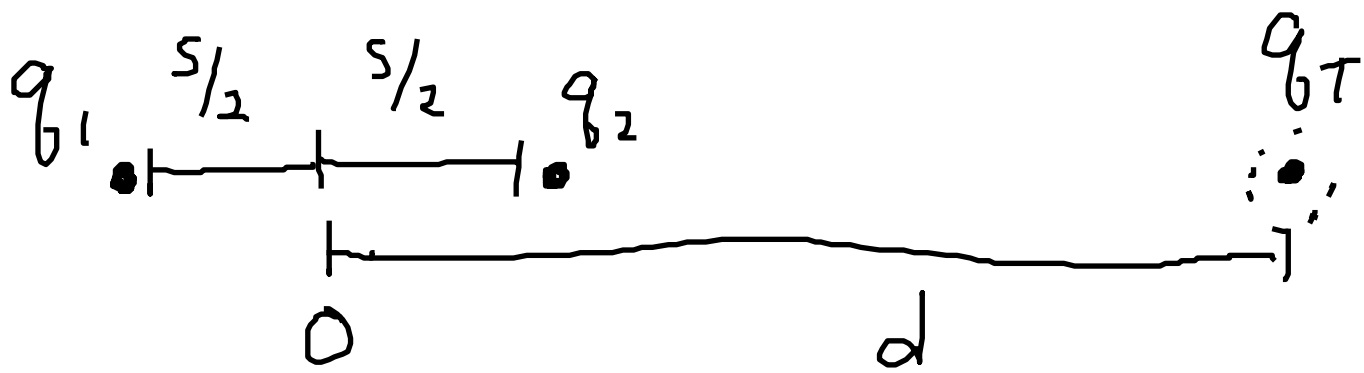


$$\vec{F} = k \frac{q_s q_t}{d^2} \hat{d} = k \frac{q_s q_t}{d^3} \vec{d}$$

$\vec{d}$ points from source to target

$$|\vec{d}| = d$$





$$\vec{F}_1 = k \frac{q_1 q_T}{\left(d + \frac{s}{2}\right)^2} \hat{x}$$

$$= k \frac{q_1 q_T}{\left(d + \frac{s}{2}\right)^2} \hat{x}$$

$$\vec{F}_2 = k \frac{q_2 q_T}{\left(d - \frac{s}{2}\right)^2} \hat{x}$$

$$\vec{F}_{\text{net}} = k \frac{q_1 q_T}{\left(d + \frac{s}{2}\right)^2} \hat{x} + k \frac{q_2 q_T}{\left(d - \frac{s}{2}\right)^2} \hat{x}$$

Taylor Expansion

epsilon, $\epsilon \ll 1$

$$(1 + \epsilon)^n \approx 1 + n\epsilon$$

$$(1 + \epsilon)^2 = 1 + 2\epsilon + \cancel{\epsilon^2}$$

$$\epsilon \ll 1, \quad \epsilon^2 \ll \ll 1$$

$$(1 + \epsilon)^3 = 1 + 3\epsilon + \cancel{3\epsilon^2} + \cancel{\epsilon^3}$$

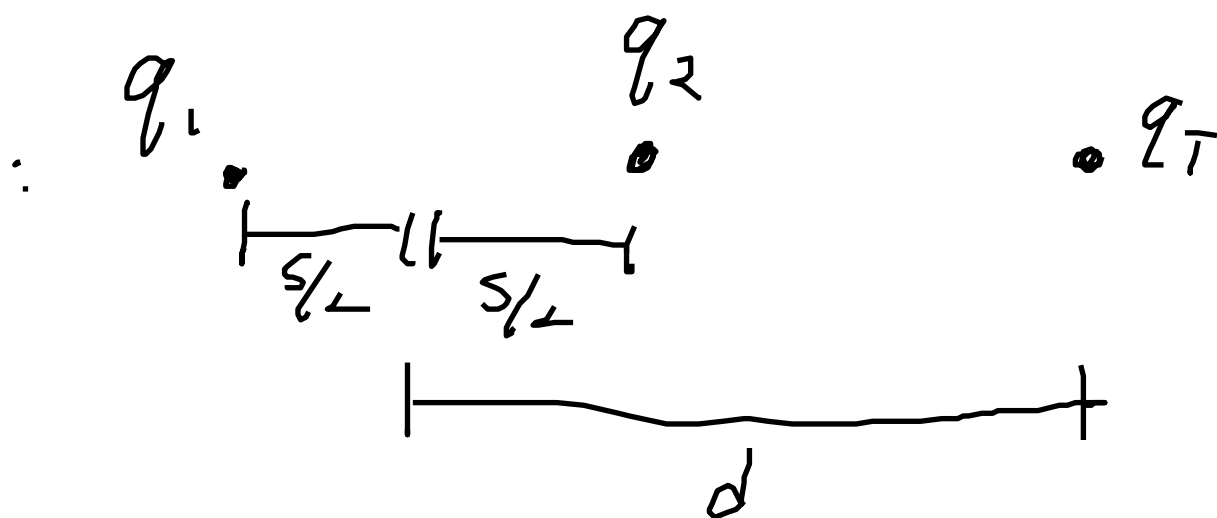
very very small

$$\frac{1}{1 + \epsilon} = (1 + \epsilon)^{-1} \approx 1 - \epsilon$$

$$\sqrt{1 + \epsilon} \approx 1 + \frac{1}{2}\epsilon$$

$$(a + \epsilon)^n = a^n \left(1 + \frac{\epsilon}{a}\right)^n =$$

$$\begin{aligned}
 (a+\epsilon)^n &= a^n \left(1 + \frac{\epsilon}{a}\right)^n \\
 &\approx a^n \left(1 + n \frac{\epsilon}{a}\right) \\
 &= a^n + n a^{n-1} \epsilon
 \end{aligned}$$



$$\begin{aligned}
 \vec{F}_{\text{net}} &= k \frac{q_1 q_T}{(d + s/2)^2} \hat{x} + k \frac{q_2 q_T}{(d - s/2)^2} \hat{x} \\
 &= k q_T \hat{x} \left[\frac{q_1}{(d + s/2)^2} + \frac{q_2}{(d - s/2)^2} \right] \\
 &= k q_T \hat{x} \left[q_1 \left(d + \frac{s}{2}\right)^{-2} + q_2 \left(d - \frac{s}{2}\right)^{-2} \right]
 \end{aligned}$$

Suppose $s \ll d$

$$a = d \quad n = -2 \quad \epsilon = \frac{s}{2}$$

$$\begin{aligned} \vec{F}_{\text{net}} &\approx k q_T \hat{x} \left[q_1 \left(d^{-2} - 2d^{-3} \frac{s}{2} \right) \right. \\ &\quad \left. + q_2 \left(d^{-2} - 2d^{-3} \left(-\frac{s}{2} \right) \right) \right] \\ &= k q_T \hat{x} \left[\frac{q_1}{d^2} + \frac{q_2}{d^2} - \frac{2}{d^3} \frac{s}{2} (q_1 - q_2) \right] \end{aligned}$$

If we ignore s term completely

$$\vec{F}_{\text{net}} = k \frac{(q_1 + q_2) q_T}{d^2} \hat{x}$$



Far enough away, treat q_1 & q_2 as a single charge

Any collection of charges
acts like a single charge
if you're far enough away
except...

$$q_1 = q \quad q_2 = -q$$

red term is zero

$$\vec{F}_{\text{net}} \approx k q_T \hat{x} \left[-\frac{s}{d^3} (q - (-q)) \right]$$

$$= k q_T \frac{2qs}{d^3} (-\hat{x})$$

$\begin{matrix} + & - \\ \bullet & \bullet \end{matrix}$ $\vec{r}$
 Electric dipole
 two opposite charges $F_{\text{net}} \sim \frac{1}{d^3}$



← dies away
faster than
point charge