

Point Charges



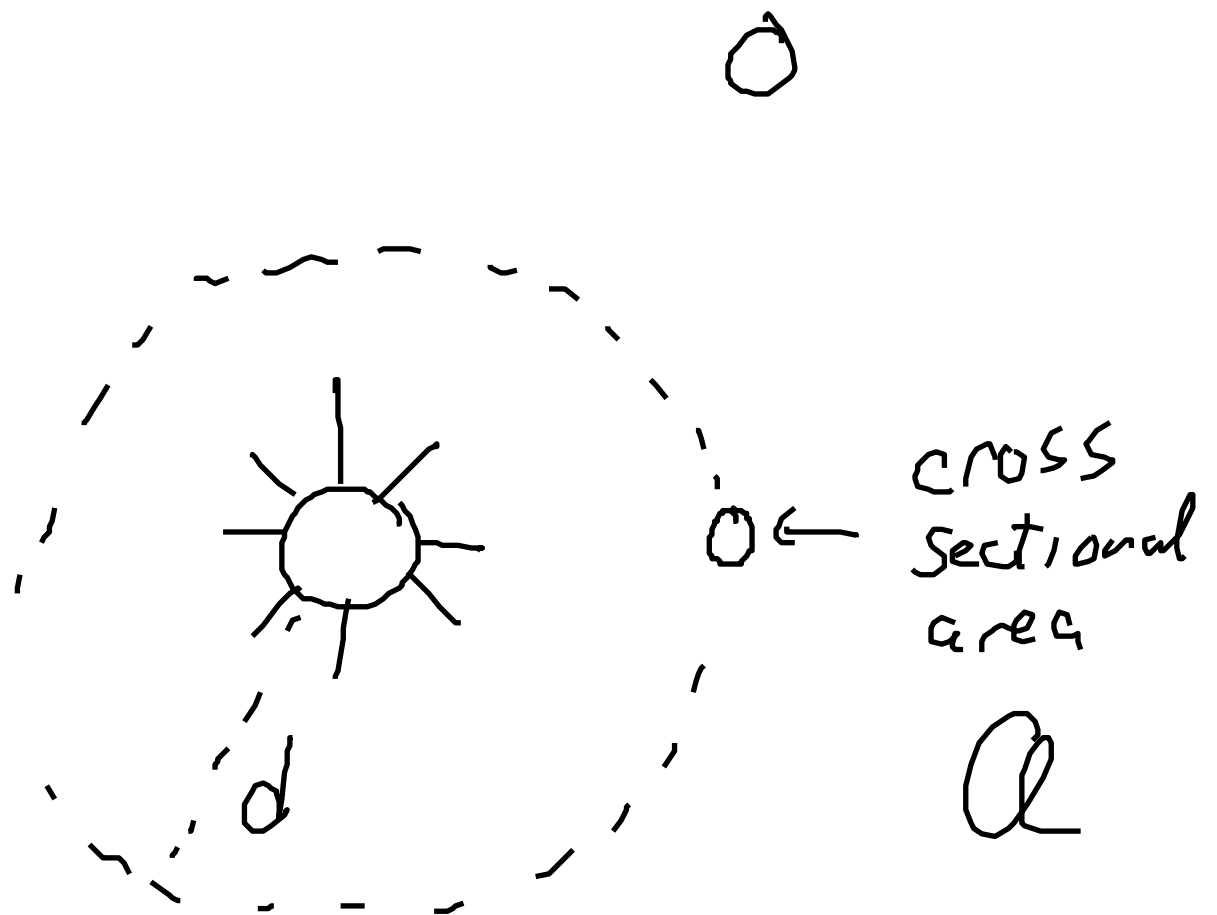
$$|\vec{F}| = F = k \frac{|q_1 q_2|}{d^2}$$

Coulomb's Law

- q_1, q_2 are charges in Coulombs (C)
- d : distance between charges
- $k = 9 \times 10^9 \frac{\text{Nm}^2}{\text{C}^2}$

Coulomb's constant

Optional



Sun puts out power L

All of light passes through sphere

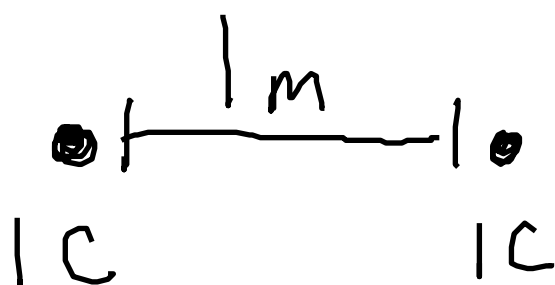
Amount of light seen by

detector is $L \frac{a}{4\pi d^2}$

Source of inverse-square law

$$F = k \frac{|q_1 q_2|}{d^2}$$

$$k = 9 \times 10^9 \frac{\text{Nm}^2}{\text{C}^2}$$



$$F = (9 \times 10^9) \frac{(1)(1)}{(1)^2}$$

$$= 9 \times 10^9 \text{ N}$$

$$= 9 \text{ billion N}$$

$$= 9 \text{ GN}$$

Average humans weight 1000 N

Coulombs are huge

$$1 \text{ mC} = 10^{-3} \text{ C}$$

milli

$$1 \mu \text{ C} = 10^{-6} \text{ C}$$

micro

$$1 \text{ nC} = 10^{-9} \text{ C}$$

nano

$$e = 1.6 \times 10^{-19} \text{ C}$$

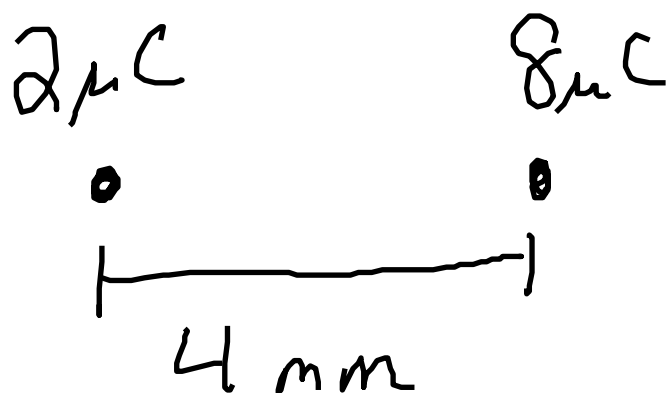
$$= 0.16 \text{ aC}$$

atto

$$\text{"m"} = \text{"} \times 10^{-3} \text{"}$$

$$\text{"}\mu\text{"} = \text{"} \times 10^{-6} \text{"}$$

$$5 \mu \text{ C} \rightarrow 5 \times 10^{-6} \text{ C}$$



Find F on either charge.

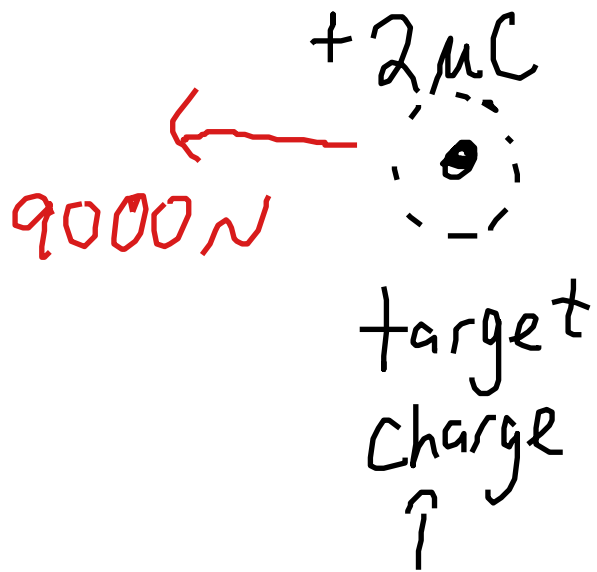
$$F = k \frac{|q_1 q_2|}{d^2}$$

$$= (9 \times 10^9) \frac{(2 \times 10^{-6})(8 \times 10^{-6})}{(4 \times 10^{-3})^2}$$

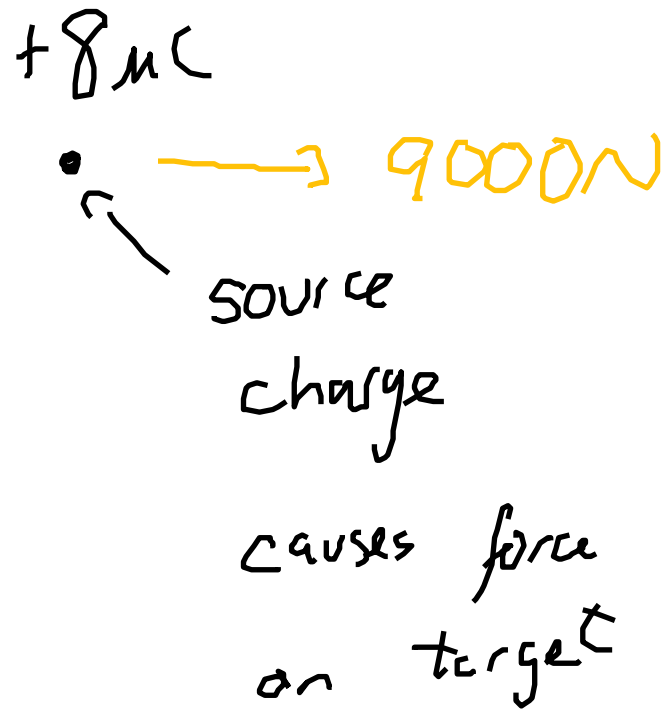
$$= 9 \times 10^9 \frac{16 \times 10^{-12}}{16 \times 10^{-6}}$$

$$= 9 \times 10^{9-12+6} = 9000\text{ N}$$

$$\sim 10,000\text{ N}$$



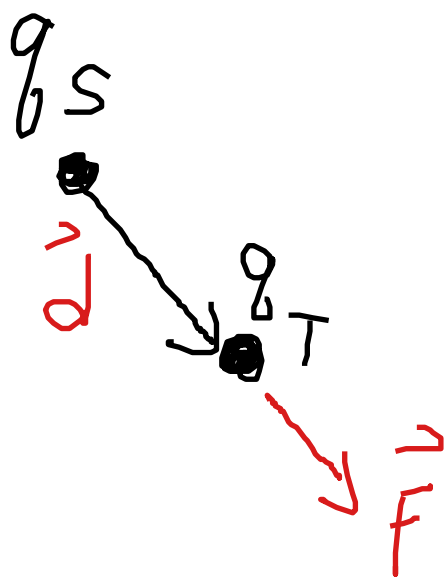
the one we
choose to
study, that
receives forces





d : points from source to target

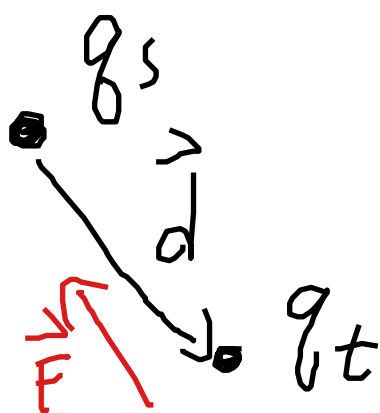
always



Both + or -

$$q_s q_t > 0$$

$$\vec{F} \sim \vec{d}$$



+ & -

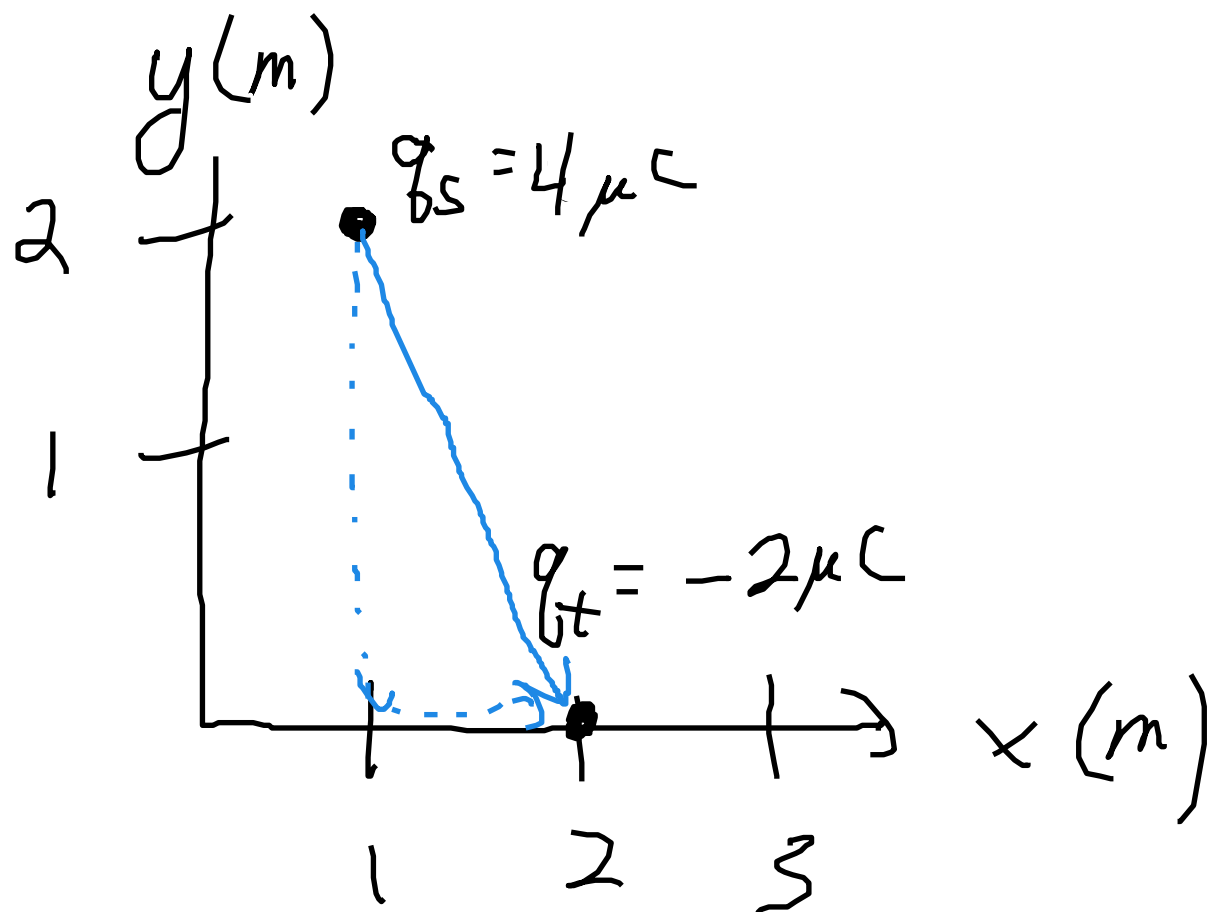
$$q_s q_t < 0$$

$$\vec{F} \sim -\vec{d}$$

$$\vec{F} = k \frac{q_s q_t}{d^2} \underbrace{\frac{\vec{d}}{d}}_{\substack{\text{Unit} \\ \text{vector}}} \\ = k \frac{q_s q_t}{d^3} \vec{d}$$

Vector form of

Coulomb's Law



What is $\vec{d}$?

$$1\hat{i} - 2\hat{j}$$

$$\langle 1, -2 \rangle$$

$$1\hat{x} - 2\hat{y}$$

$$d = |\vec{d}| = \sqrt{(1)^2 + (-2)^2} = \sqrt{5} \text{ m}$$

$$F = (9 \times 10^9) \frac{(4 \times 10^{-6})(-2 \times 10^{-6})}{(\sqrt{5})^3} (\hat{x} - 2\hat{y})$$

$$= -0.006 \text{ N } (\hat{x} - 2\hat{y})$$

$$= 0.006 \text{ N } (-\hat{x} + 2\hat{y})$$